## [Grant-in-Aid for Scientific Research (S)]

Science and Engineering (Mathematical and Physical Sciences)



Title of Project : New development of mathematical theory of turbulence by collaboration of the nonlinear analysis and computational fluid dynamics

of

and

Hideo Kozono (Waseda University, Faculty of Science and Engineering, Professor)

Research Project Number : 16H06339 Researcher Number : 00195728 Research Area : Partial Differential Equations, Nonlinear Analysis Keyword : Navier-Stokes Equations, Harmonic Analysis, Functional Analysis, Global Well-posedness, Asymptotic Analysis [Purpose and Background of the Research] We will improve a poor turbulence theory The Navier-Stokes equations have been without rigorously mathematical convention, investigated widely in both theoretical and experimental fields. The mathematical study on the and then construct a new knowledge information turbulence with abridgement Navier-Stokes equations was founded by Leray. technique. The principal investigator Kozono and Kagei As a result, reliable turbulence theory which do obtained several remarkable results in area of pure not depend on a law learned by experience or by mathematical analysis.It turns out that the intuition excessively will be largely accelerated. numerical simulation recently gives corresponding results which guarantee from viewpoint of fluid dynamics. In comparison with the numerical **[**Expected Research Achievements and simulation, the advantage of the technique of harmonic analysis makes it possible to handle the Scientific Significance It is well-known that the Clay Math. Institute asymptotic behavior of physical quantities as the proposes seven important Millennium problems, parameter goes to infinity. where the existence of the global classic solution Such a mathematical method to deal with the exact to the Navier-Stokes equations is selected. On the other hand, our DNS of the uniformly quantity as the limit of those in finite regions gives us an essential breakthrough in the numerical isotropic turbulence is by far the larger simulation in theory of turbulence. computational performance so that it can deal together with On the other hand, Kaneda with the turbulent fluid with the high Reynolds Yoshimatsu has performed of the computational number without any error of the experiment and science and statistical theory of turbulence study. indeterminacy. He has the results on the realization of the Direct Our study is based on the DNS of such a world Numerical Simulation (=DNS) in the world highest standard of Kaneda's research group, and maximum scale about the uniformly isotropic we are going to overcome difficulty of turbulence turbulence. In addition, he proceeds to the DNS of with the high Reynolds number. the high Reynolds number with the world maximum In this way, our research projects develop the size about the turbulence between two parallel flat modern mathematical analysis, the applied boards. mathematics, computational science Kaneda is evaluated as the leader developing the hydrodynamics and will lead the relevant spectrum statistics theory of turbulence. subjects to the world-wide level. [Research Methods] This project aims to establish a new theory of nonlinear dynamics for super large degree of [Publications Relevant to the Project] • Kozono, Harmonic analytic research on stationary and nonstationary problems for the freedom including the turbulence in the fluid mechanics in terms of the nonlinear analysis and incompressible Navier-Stokes equation. the computational fluid dynamics. So, we propose the following four projects (i), (ii), (iii) and (iv); (Japanese) Sugaku 67 (2015), no. 2, 113-132. • Kozono, Amann, Giga etal., Recent (i) Harmonic analysis, singular limit and estimates of effect on the finiteness Developments of Mathematical Fluid Mechanics, Birkhaeser-Verlag 2016. (ii) Mathematical analysis of boundary layer and viscosity limit (iii) Elucidation of the universal law turbulence; small and large scales of **Term of Project** FY2016-2020 (iv)Information abridgement technique, **(Budget Allocation)** 123,600 Thousand Yen prediction possibility and reliable evaluation The method dealing with infinity and the mathematical analysis such as the limiting [Homepage Address and Other Contact **Information** procedure give us the elucidation of the http://www.math.sci.waseda.ac.jp/math/ turbulence phenomenon requiring a large-scale calculation.